

2015 AMC 10A Problems

Contents

- 1 Problem 1
- 2 Problem 2
- 3 Problem 3
- 4 Problem 4
- 5 Problem 5
- 6 Problem 6
- 7 Problem 7
- 8 Problem 8
- 9 Problem 9
- 10 Problem 10
- 11 Problem 11
- 12 Problem 12
- 13 Problem 13
- 14 Problem 14
- 15 Problem 15
- 16 Problem 16
- 17 Problem 17
- 18 Problem 18
- 19 Problem 19
- 20 Problem 20
- 21 Problem 21
- 22 Problem 22
- 23 Problem 23
- 24 Problem 24
- 25 Problem 25
- 26 See also

Problem 1

What is the value of $(2^0 - 1 + 5^2 + 0)^{-1} \times 5$?

- (A) -125 (B) -120 (C) $\frac{1}{5}$ (D) $\frac{5}{24}$ (E) 25

Solution

Problem 2

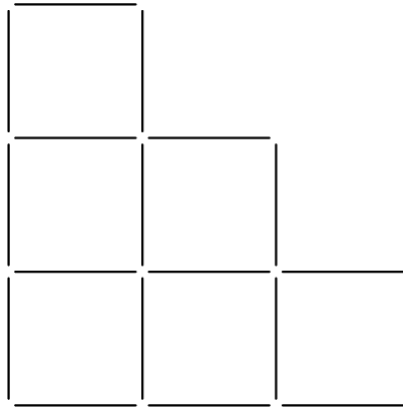
A box contains a collection of triangular and square tiles. There are 25 tiles in the box, containing 84 edges total. How many square tiles are there in the box?

- (A) 3 (B) 5 (C) 7 (D) 9 (E) 11

Solution

Problem 3

Ann made a 3-step staircase using 18 toothpicks as shown in the figure. How many toothpicks does she need to add to complete a 5-step staircase?



- (A) 9 (B) 18 (C) 20 (D) 22 (E) 24

Solution

Problem 4

Pablo, Sofia, and Mia got some candy eggs at a party. Pablo had three times as many eggs as Sofia, and Sofia had twice as many eggs as Mia. Pablo decides to give some of his eggs to Sofia and Mia so that all three will have the same number of eggs. What fraction of his eggs should Pablo give to Sofia?

- (A) $\frac{1}{12}$ (B) $\frac{1}{6}$ (C) $\frac{1}{4}$ (D) $\frac{1}{3}$ (E) $\frac{1}{2}$

Solution

Problem 5

Mr. Patrick teaches math to 15 students. He was grading tests and found that when he graded everyone's test except Payton's, the average grade for the class was 80. After he graded Payton's test, the test average became 81. What was Payton's score on the test?

- (A) 81 (B) 85 (C) 91 (D) 94 (E) 95

Solution

Problem 6

The sum of two positive numbers is 5 times their difference. What is the ratio of the larger number to the smaller number?

- (A) $\frac{5}{4}$ (B) $\frac{3}{2}$ (C) $\frac{9}{5}$ (D) 2 (E) $\frac{5}{2}$

Solution

Problem 7

How many terms are there in the arithmetic sequence 13, 16, 19, ..., 70, 73?

- (A) 20 (B) 21 (C) 24 (D) 60 (E) 61

Solution

Problem 8

Two years ago Pete was three times as old as his cousin Claire. Two years before that, Pete was four times as old as Claire. In how many years will the ratio of their ages be 2:1?

- (A) 2 (B) 4 (C) 5 (D) 6 (E) 8

Solution

Problem 9

Two right circular cylinders have the same volume. The radius of the second cylinder is 10% more than the radius of the first. What is the relationship between the heights of the two cylinders?

- (A) The second height is 10% less than the first.
(B) The first height is 10% more than the second.
(C) The second height is 21% more than the first.
(D) The first height is 21% more than the second.
(E) The second height is 80% of the first.

Solution

Problem 10

How many rearrangements of $abcd$ are there in which no two adjacent letters are also adjacent letters in the alphabet? For example, no such rearrangements could include either ab or ba .

- (A) 0 (B) 1 (C) 2 (D) 3 (E) 4

Solution

Problem 11

The ratio of the length to the width of a rectangle is $4:3$. If the rectangle has diagonal of length d , then the area may be expressed as kd^2 for some constant k . What is k ?

- (A) $\frac{2}{7}$ (B) $\frac{3}{7}$ (C) $\frac{12}{25}$ (D) $\frac{16}{25}$ (E) $\frac{3}{4}$

Solution

Problem 12

Points $(\sqrt{\pi}, a)$ and $(\sqrt{\pi}, b)$ are distinct points on the graph of $y^2 + x^4 = 2x^2y + 1$. What is $|a - b|$?

- (A) 1 (B) $\frac{\pi}{2}$ (C) 2 (D) $\sqrt{1 + \pi}$ (E) $1 + \sqrt{\pi}$

Solution

Problem 13

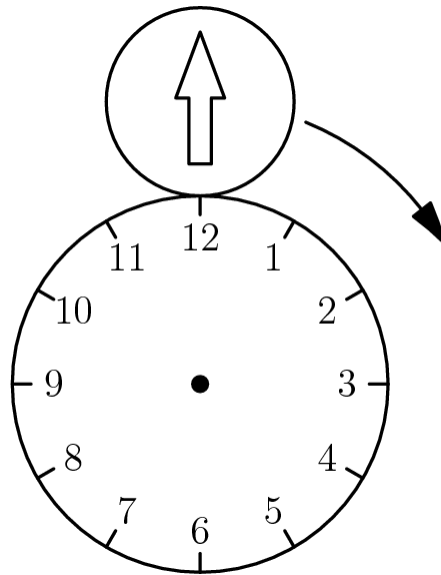
Claudia has 12 coins, each of which is a 5-cent coin or a 10-cent coin. There are exactly 17 different values that can be obtained as combinations of one or more of her coins. How many 10-cent coins does Claudia have?

- (A) 3 (B) 4 (C) 5 (D) 6 (E) 7

Solution

Problem 14

The diagram below shows the circular face of a clock with radius 20 cm and a circular disk with radius 10 cm externally tangent to the clock face at 12 o'clock. The disk has an arrow painted on it, initially pointing in the upward vertical direction. Let the disk roll clockwise around the clock face. At what point on the clock face will the disk be tangent when the arrow is next pointing in the upward vertical direction?



- (A) 2 o'clock (B) 3 o'clock (C) 4 o'clock (D) 6 o'clock (E) 8 o'clock

Solution

Problem 15

Consider the set of all fractions $\frac{x}{y}$, where x and y are relatively prime positive integers. How many of these fractions have the property that if both numerator and denominator are increased by 1, the value of the fraction is increased by 10%?

- (A) 0 (B) 1 (C) 2 (D) 3 (E) infinitely many

Solution

Problem 16

If $y + 4 = (x - 2)^2$, $x + 4 = (y - 2)^2$, and $x \neq y$, what is the value of $x^2 + y^2$?

- (A) 10 (B) 15 (C) 20 (D) 25 (E) 30

Solution

Problem 17

A line that passes through the origin intersects both the line $x = 1$ and the line $y = 1 + \frac{\sqrt{3}}{3}x$. The three lines create an equilateral triangle. What is the perimeter of the triangle?

- (A) $2\sqrt{6}$ (B) $2 + 2\sqrt{3}$ (C) 6 (D) $3 + 2\sqrt{3}$ (E) $6 + \frac{\sqrt{3}}{3}$

Solution

Problem 18

Hexadecimal (base-16) numbers are written using numeric digits 0 through 9 as well as the letters A through F to represent 10 through 15. Among the first 1000 positive integers, there are n whose hexadecimal representation contains only numeric digits. What is the sum of the digits of n ?

- (A) 17 (B) 18 (C) 19 (D) 20 (E) 21

Solution

Problem 19

The isosceles right triangle ABC has right angle at C and area 12.5 . The rays trisecting $\angle ACB$ intersect AB at D and E . What is the area of $\triangle CDE$?

- (A) $\frac{5\sqrt{2}}{3}$ (B) $\frac{50\sqrt{3} - 75}{4}$ (C) $\frac{15\sqrt{3}}{8}$ (D) $\frac{50 - 25\sqrt{3}}{2}$ (E) $\frac{25}{6}$

Solution

Problem 20

A rectangle with positive integer side lengths in cm has area A cm² and perimeter P cm. Which of the following numbers cannot equal $A + P$?

- (A) 100 (B) 102 (C) 104 (D) 106 (E) 110

NOTE: As it originally appeared in the AMC 10, this problem was stated incorrectly and had no answer; it has been modified here to be solvable.

Solution

Problem 21

Tetrahedron $ABCD$ has $AB = 5$, $AC = 3$, $BC = 4$, $BD = 4$, $AD = 3$, and $CD = \frac{12}{5}\sqrt{2}$. What is the volume of the tetrahedron?

- (A) $3\sqrt{2}$ (B) $2\sqrt{5}$ (C) $\frac{24}{5}$ (D) $3\sqrt{3}$ (E) $\frac{24}{5}\sqrt{2}$

Solution

Problem 22

Eight people are sitting around a circular table, each holding a fair coin. All eight people flip their coins and those who flip heads stand while those who flip tails remain seated. What is the probability that no two adjacent people will stand?

- (A) $\frac{47}{256}$ (B) $\frac{3}{16}$ (C) $\frac{49}{256}$ (D) $\frac{25}{128}$ (E) $\frac{51}{256}$

Solution

Problem 23

The zeroes of the function $f(x) = x^2 - ax + 2a$ are integers. What is the sum of the possible values of a ?

- (A) 7 (B) 8 (C) 16 (D) 17 (E) 18

Solution

Problem 24

For some positive integers p , there is a quadrilateral $ABCD$ with positive integer side lengths, perimeter p , right angles at B and C , $AB = 2$, and $CD = AD$. How many different values of $p < 2015$ are possible?

- (A) 30 (B) 31 (C) 61 (D) 62 (E) 63

Solution

Problem 25

Let S be a square of side length 1. Two points are chosen at random on the sides of S . The probability that the straight-line distance between the points is at least $\frac{1}{2}$ is $\frac{a-b\pi}{c}$, where a , b , and c are positive integers with $\gcd(a, b, c) = 1$. What is $a + b + c$?

- (A) 59 (B) 60 (C) 61 (D) 62 (E) 63

Solution

See also

2015 AMC 10A (Problems • Answer Key • Resources)	
Preceded by 2014 AMC 10B Problems	Followed by 2015 AMC 10B Problems
1 • 2 • 3 • 4 • 5 • 6 • 7 • 8 • 9 • 10 • 11 • 12 • 13 • 14 • 15 • 16 • 17 • 18 • 19 • 20 • 21 • 22 • 23 • 24 • 25	
All AMC 10 Problems and Solutions	

- AMC 10
- AMC 10 Problems and Solutions
- 2015 AMC 10A
- Mathematics competition resources

The problems on this page are copyrighted by the Mathematical Association of America's American Mathematics

Competitions.



Retrieved from "http://artofproblemsolving.com/wiki/index.php?title=2015_AMC_10A_Problems&oldid=87964"

Copyright © 2018 Art of Problem Solving